“A programming language is low level when its programs require attention to the irrelevant.”

Alan Perlis
Before We Get Started…

- **Last Time**
  - OpenMP wrap up
    - Variable scoping example
    - OpenMP API
  - A critical look at CUDA, OpenMP, MPI

- **Today**
  - Parallel programming patterns
  - One slide summary of ME964

- **Other issues:**
  - Choose time slot, Final Project presentation: [http://www.doodle.com/3b65mca99d6wuety](http://www.doodle.com/3b65mca99d6wuety)
    - Potential conflict: It looks like on Th, May 17, 10 -11:30 am I’m going to be in a PhD Prelim Exam
  - Two guest lectures next week
Recommended Reading


- Used for this presentation
- An overview of challenges, best practices, and common techniques in all aspects of parallel programming
- Book is on reserve at Wendt Library
Objectives

- Get exposed to techniques & best practices that have emerged as useful in the parallel programming practice
- They are expected to facilitate and/or help you with
  - Thinking about/Visualizing your problem as you try to design a parallel implementation for its solution
  - Addressing functionality and performance issues in your parallel program design
  - Discussing your design decisions with others
  - Selecting an appropriate platform that helps you express & implement the parallel design for the solution you identified
Parallel Computing: When and Why.

- Parallel computing, prerequisites
  - The problem can be decomposed into sub-problems that can be independently solved at the same time
  - The part of the problem that is concurrent is large enough to justify an approach that exploits this concurrency
    - Recall Amdhal’s law

- Parallel computing: Why?
  - Solve problems in less time
    - and/or
  - Solve bigger problems
Parallel Computing, Caveats

- Performance can be drastically reduced by several factors
  - Overhead of parallel processing
  - Load imbalance among processor elements
  - Inefficient data sharing patterns
  - Saturation of critical resources such as memory bandwidth
Implementing a Parallel Solution to Your Problem: Key Steps

1) Find the concurrency in the problem

2) Structure the algorithm so that concurrency can be exploited

3) Implement the algorithm in a suitable programming environment

4) Tune the performance of the code on the target parallel system

NOTE: The reality is that these have not been separated into levels of abstractions that can be dealt with independently.
(“Whenever anyone says, 'theoretically,' they really mean, 'not really.’” Dave Parnas)
What’s Next?

Focus on this for a while

Finding Concurrency

Algorithm Structure

Supporting Infrastructure

Implementation Mechanisms

From “Patterns for Parallel Programming”
Finding and Nurturing Concurrency

- Dependence kills concurrency. Dependencies need to be identified and managed
  - Dependencies prevent parallelism, at least the “embarrassingly parallel” flavor
  - Often times, dependencies end up requiring synchronization barriers (not good…)

- Concurrency has some caveats (heads up)
  - In sequential execution one thing is clear: One step feeds result to the next steps ⇒ a unique way moving from A to Z
  - In parallel execution: numeric accuracy may be affected by ordering steps that parallel with each other ⇒ platform dependent, OS dependent, possibly even dependent on the state of the system

- Finding and exploiting concurrency often requires looking at the problem from a non-obvious angle
Finding Concurrency in Problems

- Goal: Identify a decomposition of the problem into sub-problems that can be solved simultaneously

- In order to meet this goal:
  - Perform a task decomposition to identify tasks that can execute concurrently
  - Carry out data decomposition to identify whether you can create a task around data
  - Identify task grouping and group ordering to satisfy temporal constraints
  - Carry out an analysis of the data sharing patterns among the concurrent tasks to avoid any race condition issues and optimize memory access
  - Perform a design evaluation that assesses the quality of the choices made in all the steps
Finding Concurrency – The Process

This is typically an iterative process, like an optimization process that has to negotiate several constraints.
Find Concurrency 1: Decomp. Stage: Task Decomposition

- Many large problems have natural independent tasks

  - The number of tasks considered should correlate with the execution resources available.

  - Each task must include sufficient work in order to compensate for the overhead of managing their parallel execution.

  - Tasks should attempt to maximize reuse of sequential program code to minimize design/implementation effort.

“In an ideal world, the compiler would find tasks for the programmer. Unfortunately, this almost never happens.”
- Mattson, Sanders, Massingill
Example: Task Decomposition Square Matrix Multiplication

- $P = M \times N$ of $\text{WIDTH} \times \text{WIDTH}$
  - One natural task (sub-problem) produces one element of $P$
  - All tasks can execute in parallel
Find Concurrency 2: Decomp. Stage: Data Decomposition

- The most compute intensive parts of many large problems manipulate a large data structure
  - Similar operations are being applied to different parts of the data structure, in a mostly independent manner
  - “If a program manipulates a large amount of data, it does so in a small number of ways.” (Alan Perlis)

- The data decomposition should lead to
  - Efficient data usage by each Unit of Execution (UE) within the partition
  - Few dependencies between the UEs that work on different partitions
  - Adjustable partitions that can be varied according to the hardware characteristics
Sometimes several tasks in problem can be grouped to improve efficiency

- Recall the idea of operation fusing in **thrust**
- Reduced synchronization overhead – because when task grouping there is supposedly no need for synchronization
- All tasks in the group efficiently share data loaded into a common on-chip, shared storage (Shared Memory)
Task Grouping Example - Square Matrix Multiplication

- Tasks calculating a P sub-block
  - Extensive input data sharing, reduced memory bandwidth using Shared Memory
  - All synched in execution
Find Concurrency 4: Dependence Analysis - Task Ordering

- Identify the data required by a group of tasks before they can execute
  - Find the task group that creates it (look upwind)
  - Determine a temporal order that satisfy all data constraints
Task Ordering Example: Finite Element Analysis

1. Node List
2. External Forces
3. Element Internal Force
4. Acceleration of each deformable beam
5. Update position and velocity of each beam
6. Next Time Step
Find Concurrency 5: Dependence Analysis - Data Sharing

- Data sharing can be a double-edged sword
  - An algorithm that calls for excessive data sharing can drastically reduce advantage of parallel execution
  - Localized sharing can improve memory bandwidth efficiency
  - Use the execution of task groups to interleave with (mask) global memory data accesses

- Read-only sharing can usually be done at much higher efficiency than read-write sharing, which often requires a higher level of synchronization
Find Concurrency 6: Design Evaluation

- Key questions to ask

  - How many Units of Execution (UE) can be used?
  
  - How are the data structures shared?
    - Is there a lot of data dependency that leads to excessive synchronization needs?

  - Is there enough work in each UE between synchronizations to make parallel execution worthwhile?
Implementing a Parallel Solution to Your Problem: Key Steps

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From “Patterns for Parallel Programming”
Algorithm: Definition

- A step by step procedure that is guaranteed to terminate, such that each step is precisely stated and can be carried out by a computer

- Attributes of an algorithm
  - Definiteness – the notion that each step is precisely stated
  - Effective computability – each step can be carried out by a computer
  - Finiteness – the procedure terminates

- Multiple algorithms can be used to solve the same problem
  - Some require fewer steps and some exhibit more parallelism
Algorithm Structure - Strategies

Organize by Tasks
- Task Parallelism
- Divide and Conquer

Organize by Data
- Geometric Decomposition
- Recursive Data Decomposition

Organize by Flow
- Pipeline
- Event Condition
Choosing Algorithm Structure

Algorithm Design

Organize by Task
- Linear
  - Task Parallelism
- Recursive
  - Divide and Conquer

Organize by Data
- Linear
  - Geometric Decomposition
- Recursive
  - Recursive Data Decmp.

Organize by Data Flow
- Regular
  - Pipeline
- Irregular
  - Event Driven
Alg. Struct. 1: Organize by Task
Linear Parallel Tasks

- These are the algorithms where the work needed can be represented as a collection of decoupled or loosely coupled tasks that can be executed in parallel
  - The tasks don’t even have to be identical
  - Load balancing between UE can be an issue (dynamic load balancing?)
  - If there is no data dependency involved there is no need for synchronization: the so called “embarrassingly parallel” scenario

- Common in the context of distributed memory models
Alg. Struct. 1: Organize by Task
Linear Parallel Tasks [Cntd.]

Examples

- Imagine a car that needs to be painted:
  - One robot paints the front left door, another one the rear left door, another one the hood, etc.
  - The car is parceled up with a collection of UEs taking care of subtasks

- Other: ray tracing, a good portion of the N-body problem, Monte Carlo type simulation
Alg. Struct. 2: Organize by Task
Recursive Parallel Tasks (Divide & Conquer)

- Valid when you can break a problem into a set of decoupled or loosely coupled smaller problems, which in turn you can break again, etc…
  - This pattern is applicable when you can solve concurrently and with little synchronization the small problems (the leafs)

- In some case you need synchronization when dealing with this balanced tree type algorithm
  - Often required by the merging step (assembling the result from the “subresults”)

- Examples: FFT, Linear Algebra problems (see FLAME project), the vector reduce operation
Alg. Struct. 3: Organize by Data
~ Linear (Geometric Decomposition) ~

- This is the case where the UEs gather and work around a big chunk of data with little or no synchronization.

- This is exactly the algorithmic approach enabled best by the GPU & CUDA.

- Examples: Matrix multiplication, matrix convolution, image processing.
Alg. Struct. 4: Organize by Data
~ Recursive Data Scenario ~

- Scenario encountered when data you operate on is structured in a recursive fashion
  - Balanced Trees
  - Graphs
  - Lists

- Sometimes you don’t even have to have the data represented as such
  - See example with prefix scan
  - You choose to look at data as having a balanced tree structure

- Problems that seem inherently sequential can be approached in this framework
  - Typically associated with a net increase in the amount of work you have to do
  - Work goes up from $O(n)$ to $O(n \log(n))$ (see for instance Hillis and Steele algorithm)
  - The key question is whether parallelism gained puts you ahead of the sequential alternative
Example: The Prefix Scan ~ Reduction Step~

for \( k=0 \) to \( M-1 \)
\[
\text{offset} = 2^k
\]
for \( j=1 \) to \( 2^{M-k-1} \) in parallel do
\[
x[j \cdot 2^{k+1}-1] = x[j \cdot 2^{k+1}-1] + x[j \cdot 2^{k+1}-2^k-1]
\]
endfor
endfor
Example: The array reduction (the bad choice)

Array elements

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Alg. Struct. 5: Organize by Data Flow ~ Regular: Pipeline ~

- Tasks are parallel, but there is a high degree of synchronization (coordination) between the UEs
  - The input of one UE is the output of an upwind UE (the “pipeline”)
  - The time elapsed between two pipeline ticks dictated by the slowest stage of the pipeline (the bottleneck)

- Commonly employed by sequential chips

- For complex problems, having a deep pipeline is attractive
  - At each pipeline tick you output one set of results

- Examples:
  - CPU: instruction fetch, decode, data fetch, instruction execution, data write are pipelined
  - The Cray vector architecture drawing heavily on this algorithmic structure when performing linear algebra operations
Alg. Struct. 6: Organize by Data Flow
~ Irregular: Event Driven Scenarios ~

- Examples: computer games, traffic control algorithms, server operation (amazon, google, priceline)

- Well supported by MIMD architectures in hardware and OpenMP (through tasks/sections) in software
  - The furthest away from what the GPU can support today

- You coordinate UEs through asynchronous events

- Critical aspects:
  - Load balancing – should be dynamic
  - Communication overhead, particularly in real-time applications

- Suitable for action-reaction type simulations
Implementing a Parallel Solution to Your Problem: Key Steps

1) Find the concurrency in the problem

2) Structure the algorithm so that concurrency can be exploited

3) **Implement the algorithm in a suitable programming environment**

4) Execute and tune the performance of the code on a parallel system
What’s Comes Next?

Focus on this for a while

Finding Concurrency

Algorithm Structure

Supporting Infrastructure

Implementation Mechanisms
Implement Algorithm in Suitable Programming Environment

Below are the models for which parallel software/hardware combos provide good support nowadays. If you don’t fall in one of the above there’ll be no sailing, you’ll have to row.
Data Models

- **Shared Data**
  - All threads share a major data structure
  - This is what CUDA & GPU computing support the best

- **Shared Queue**
  - All threads see a “thread safe” queue
  - Very relevant in conjunction with the Master/Worker scenarios
  - OpenMP & Many-core very helpful here if your problem fits on one machine
    - If not, MPI can help

- **Distributed Array**
  - Decomposed and distributed among threads
  - MPI & Cray, or MPI & IBM
  - Good library support under MPI (this is how things get done in PETSc)
Program Models

- **Master/Worker**
  - A Master thread sets up a pool of worker threads and a bag of tasks
  - Workers execute concurrently, removing tasks until done
  - Common in OpenMP

- **Loop Parallelism**
  - Loop iterations execute in parallel
  - Very common in OpenMP

- **Fork/Join**
  - Most general way of creation of threads (the POSIX standard)
  - Can be regarded as a very low level approach in which you use the OS to manage parallelism
SPMD (Single Program, Multiple Data)

- All PE’s (Processor Elements) execute the same program in parallel
- Each PE has its own data
- Each PE uses a unique ID to access its portion of data
- Different PE can follow different paths through the same code

SPMD is by far the most commonly used pattern for structuring parallel programs.
More on SPMD

- Dominant coding style of scalable parallel computing
  - MPI code is mostly developed in SPMD style
  - Almost exclusively used as the pattern in GPU computing
  - Much OpenMP code is also in SPMD
  - Particularly suitable for algorithms based on data parallelism, geometric decomposition, divide and conquer.

- Main advantage
  - Tasks and their interactions visible in one piece of source code, no need to correlated multiple sources
Typical SPMD Program Phases

- Initialize
  - Establish localized data structure and communication channels

- Obtain a unique identifier
  - Each thread acquires a unique identifier, typically in the range from 0 to N-1, where N is the number of threads.
  - OpenMP, MPI, and CUDA have built-in support for this

- Distribute Data
  - Decompose global data into chunks and localize them, or
  - Sharing/replicating major data structure using thread ID to associate subset of the data to threads

- Run the core computation
  - More details in next slide…

- Finalize
  - Reconcile global data structure, prepare for the next major iteration
Core Computation Phase

- Thread IDs are used to differentiate behavior of threads
  - CUDA: Indx.x, Indx.y, Indx.z (also block ids)
  - MPI: rank of a process
  - OpenMP: get_thread_num() – gets id associated with a specific thread in a parallel region

- Thread ID used in loop index calculations to split loop iterations among threads

- Use conditions based on thread ID to branch to their specific actions
## Parallel Programming Support vs. Program Models

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### Algorithm Structures [in columns] vs. Program Models [in rows]

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<th>Task Parallel</th>
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<th>Geometric Decomp.</th>
<th>Recursive Data</th>
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Four smilies is the best (Source: Mattson, et al.)
Sequential computing hit three walls: power, memory, and ILP walls

Moore’s law scales at least for one more decade
  Parallel computing poised to pick up where sequential computing left

Moore’s law brought us powerful GPUs and many-core CPUs
  Use OpenMP and/or CUDA (or OpenCL) to leverage this hardware

Large problems do not always fit inside one workstation
  Not enough memory, or if enough memory not enough crunching number power

Large problem handled well by clusters or massively parallel computers
  MPI helps you here

When possible, use parallel libraries (thrust, PETSc, TBB, MKL, etc.)
  However, writing your own code for your own small problem sometimes pays off nicely
End of ME964.
Thank You.
Data Sharing Example
Matrix Multiplication on the GPU

- Each task group will finish usage of each sub-block of $N$ and $M$ before moving on
  - $N$ and $M$ sub-blocks loaded into Shared Memory for use by all threads of a $P$ sub-block
  - Amount of on-chip Shared Memory strictly limits the number of threads working on a $P$ sub-block

- Read-only shared data can be efficiently accessed as Constant or Texture data (on the GPU)
  - Frees up the shared memory for other uses
Computational ordering can have major effects on memory bank conflicts and control flow divergence.