

## MATLAB Assignment 6

November 6, 2014

Due: November 13, 2014

When working on this assignment you might want to take a look at MATLAB code that was developed by students who took ME451 in previous years. The students back then did not come up with identical solutions. Take a look at their solutions and develop your own.

2010: <http://sbel.wisc.edu/Courses/ME451/2010/SimEngine2D/index.htm>

2011: <http://sbel.wisc.edu/Courses/ME451/2011/SimEngine2D/index.htm>

Turning in your assignment: place all your files in a directory called "lastName\_Matlab\_06", zip that directory, and upload the resulting file "lastName\_Matlab\_06.zip" in the appropriate Dropbox Folder at Learn@UW.

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**Problem 1.** Assume that  $\mathbf{q} = [x, y]^T$  and

$$\Phi(\mathbf{q}) = \begin{bmatrix} 3x + \sin(xy) - 4 \\ x - e^{\cos(y)} \end{bmatrix}$$

1. Compute the Jacobian (matrix of partial derivatives)  $\Phi_{\mathbf{q}}$ .
2. Write a MATLAB program that implements the Newton-Raphson method for solving the nonlinear system  $\Phi(\mathbf{q}) = \mathbf{0}$ . For the stopping criteria, use the condition that the norm of the correction should be less than  $10^{-8}$ .
3. Post on the forum the results that you get when you run the MATLAB program above using as a starting point  $\mathbf{q}^{(0)} = [1.5, 1.5]^T$ .

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**Problem 2.** Consider the pendulum at page 60 of the textbook (Example 3.2.1). Use the pair of files `simplePend.acf` and `simplePend.adm` that you generated in a previous assignment.

- a. Write a MATLAB program that parses the ADM file and then calculates the following quantities:  $\Phi$ ,  $\Phi_{\mathbf{q}}$ ,  $\nu$ , and  $\gamma$ , all evaluated at time  $t = 0$ , with  $\mathbf{q}(0) = \mathbf{q}_0$  and  $\dot{\mathbf{q}}(0) = \dot{\mathbf{q}}_0$  consistent with the given motion at  $t = 0$ . Post on the forum the values you obtain for these four quantities.
- b. Write a MATLAB program that does the following: first, it parses the ADM and ACF files to read in the model and type of analysis. Next, it runs a loop over time from  $t_0 = 0$  to the final time in increments specified in the ACF file; i.e.,  $t_{end} = 1$  and  $\Delta t = 0.01$ . At each time step  $t_1, t_2, \dots, t_{end}$ , it prints out the values of  $\Phi(\mathbf{q}, t)$ ,  $\Phi_{\mathbf{q}}(\mathbf{q}, t)$ , and  $\nu(\mathbf{q}, t)$ . On the forum, report the value that you get at  $t_{37} = 0.37$ .

**Notes:**

- As time is incremented, the values of  $x$ ,  $y$ , and  $\phi$  change so that they satisfy the constraints. Make sure you work with the correct values when you compute  $\Phi$ ,  $\Phi_{\mathbf{q}}$ , and  $\nu$ . For this assignment, you can hard-code the analytical solution of the Position Analysis Problem or simply use your `simEngine2D`.